

# Improvement of Lake Ice Thickness Retrieval From MODIS Satellite Data Using a Thermodynamic Model

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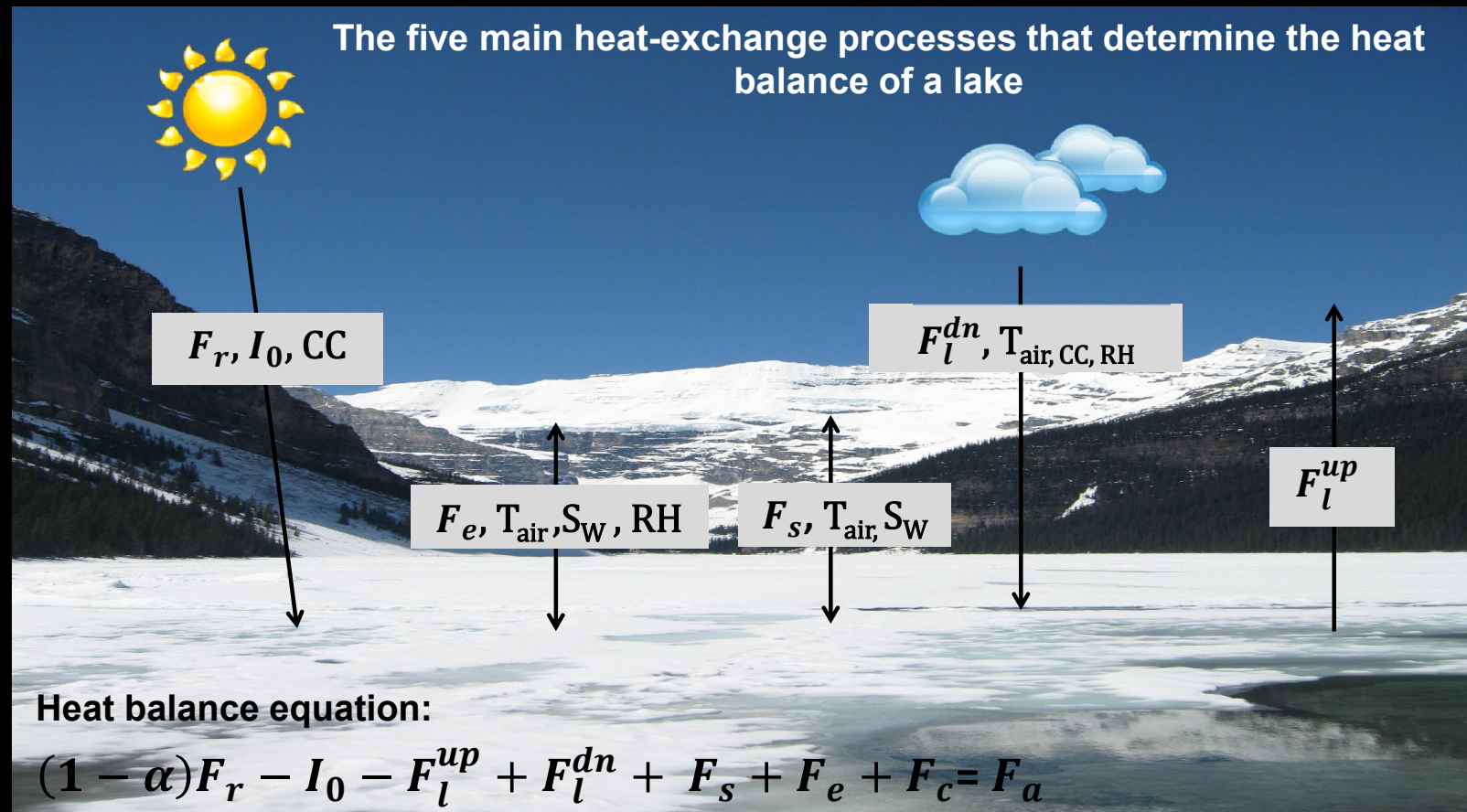
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**WATERLOO**





# Role of lake ice in regional weather and climate

Lake surface properties such as **water temperature** and **ice cover** are two important parameters when considering lake-atmosphere interactions



$\alpha$  = albedo

$I_0$  = penetration radiation through ice

$F_r$  = downward shortwave radiation

$F_l^{up}$  = upward longwave radiation

$F_l^{dn}$  = downward longwave radiation

$F_s$  = sensible Heat Flux

$F_e$  = latent heat flux

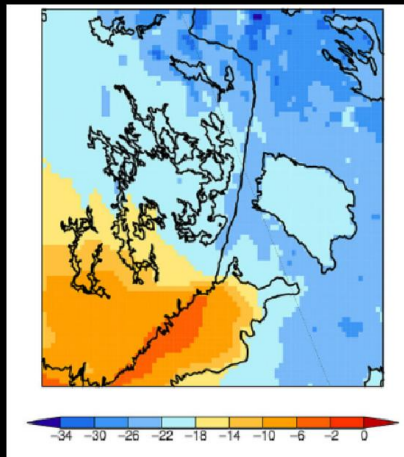
$F_c$  = conductive heat flux

$F_a$  = residual heat flux  
( $F_a$  assumed to be zero)

# Importance of ice cover monitoring

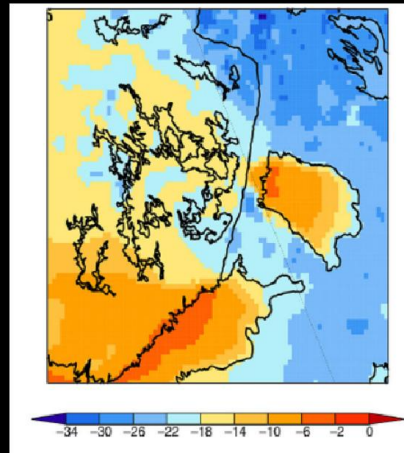
## Assimilate lake surface temperature in HIRLAM forecasting model

without LWST data

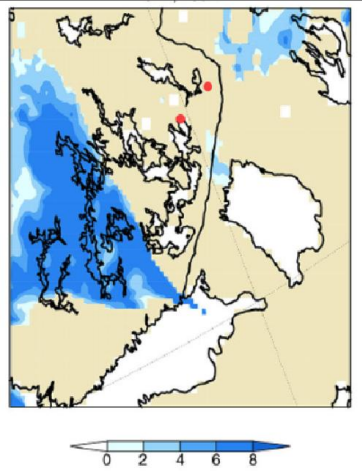


Simulated 2m air temperature

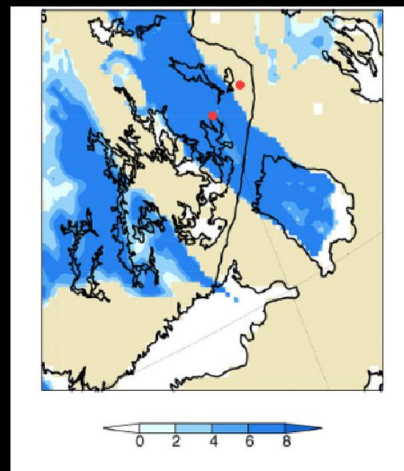
with LWST data



Simulated 2m air temperature



Simulated cloud cover



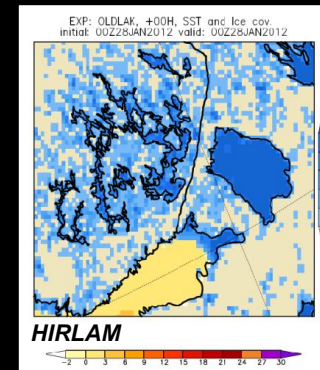
Simulated cloud cover

**HIRLAM Forecast**

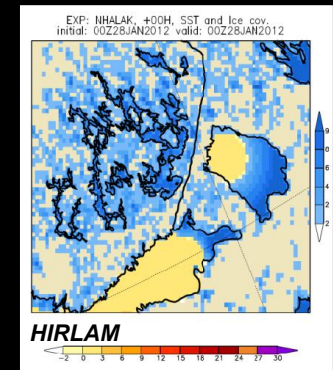


MODIS visible image  
28 January 2012  
Lake Ladoga, RU

Analyzed ice cover without assimilation



Analyzed ice cover with assimilation

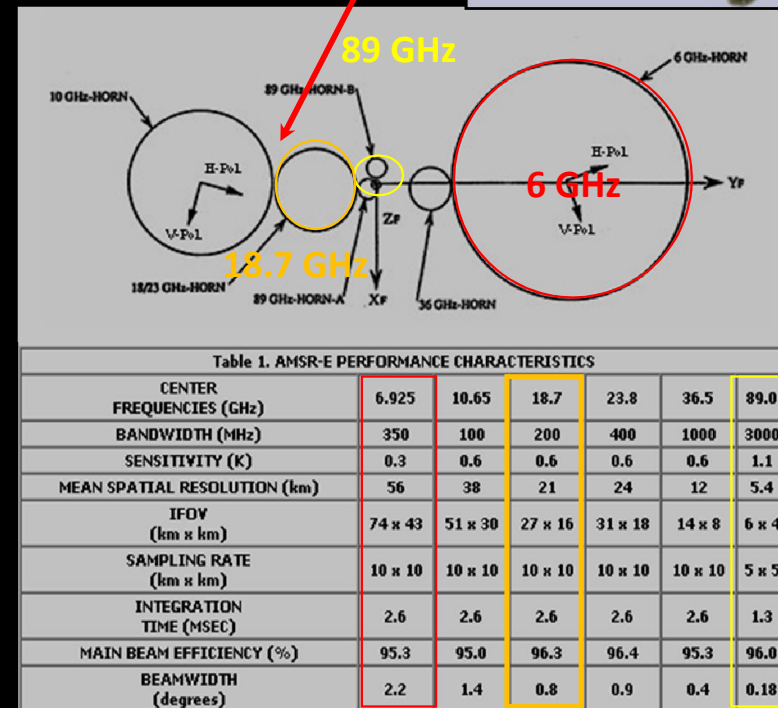
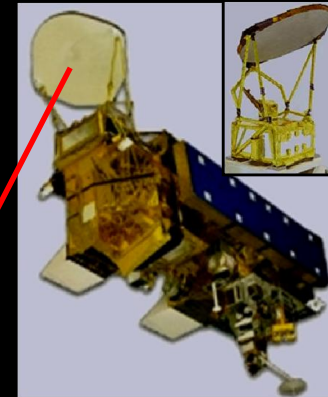


**HIRLAM Analysis**

Eerola et al., 2014  
Kheyrollah Pour et al., 2014

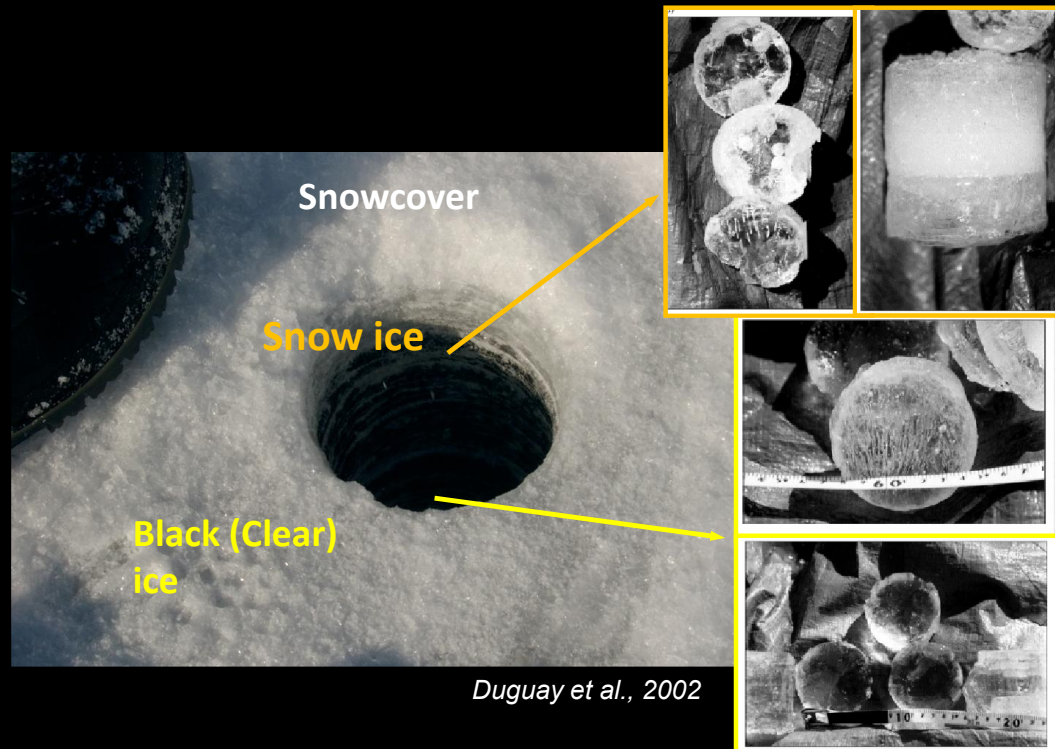
# Ice thickness retrieval using passive microwave sensors e.g. AMSR-E

- The spatial footprint of the lower frequencies of passive microwave sensors is relatively large (20–50 km) ,  
**76×44 km at 6.9 GHz**
- Higher frequencies are more sensitive to the atmosphere.
- 6×4 km at 89.0 GHz**





## *Ice thickness*



### **Snow ice**

- Rounded-shape (spherical) bubble

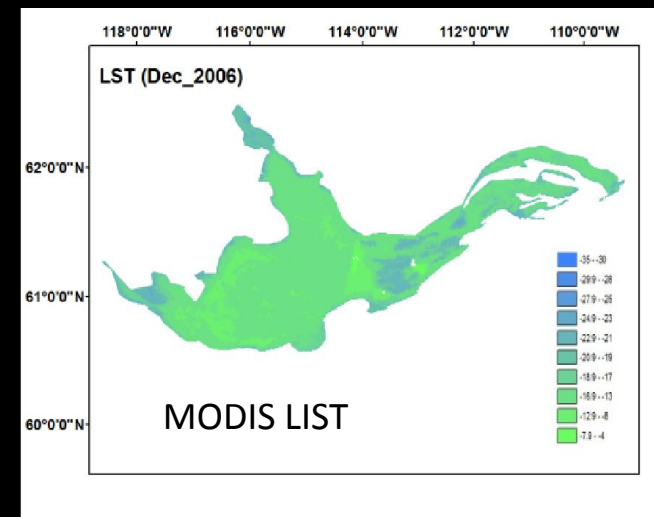
### **Black ice**

- Elongated-shape (cylindrical) bubble

Retrieval of ice thickness is challenging in high latitude regions at a time when such measurements are increasingly being requested by operational weather forecasting and ice centers

## *Motivation*

This study aimed to improve the previous approach using thermal infrared observations to estimate ice thickness. The approach is based on the use of Moderate Resolution Imaging Spectroradiometer lake ice surface temperature (MODIS LST) and with snow depth calculated by the 1-D thermodynamic Canadian Lake Ice Model (CLIMo).



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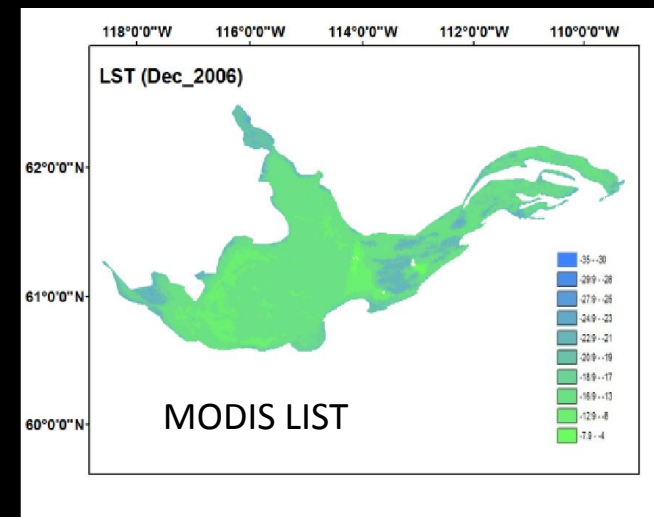
Previous studies snow depth approach:

Empirical relationship between snow and ice

$$h_s = 0 \quad \text{for } H_i < 0.05 \text{ m}$$

$$h_s = 0.05H_i \quad \text{for } 0.05 \text{ m} \leq H_i \leq 0.2 \text{ m}$$

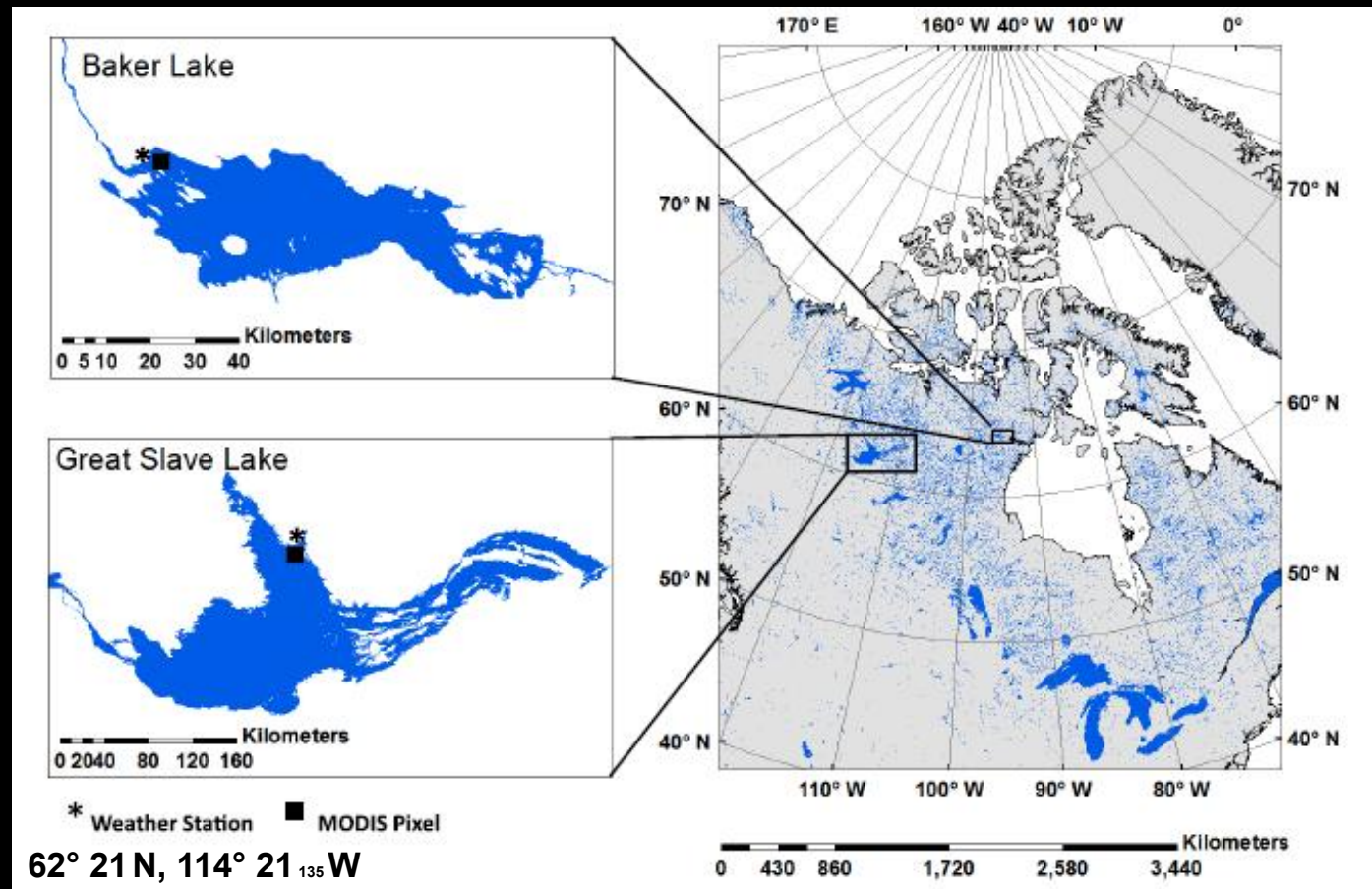
$$h_s = 0.2H_i \quad \text{for } H_i > 0.2 \text{ m.}$$



## Study area

### Great Slave and Baker Lake, Canada

- **Baker Lake, Nunavut:**
- Maximum depth: 60 m
- Area: 182.2 km<sup>2</sup>
- Covered by ice usually from **Nov.-May**
- **Great Slave Lake, NWT:**
- Maximum depth: 614 m
- Mean depth: 41 m
- Area: 27,000 km<sup>2</sup>
- Covered by ice usually from **Dec.-May**





## *Heat balance equation*

$$(1 - \alpha)F_r - I_0 - F_l^{up} + F_l^{dn} + F_s + F_e + F_c = F_a$$

$\alpha$  = albedo

$I_0$  = penetration radiation through ice

$F_r$  = downward shortwave radiation

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## Heat balance equation/ MODIS LIST

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$T_s$  = MODIS night-time LIST observations

## Heat balance equation/ MODIS LIST

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$$F_c = \gamma (T_f - T_s)$$

$T_f$  = freezing temperature

$T_s$  = MODIS night-time LIST observations

$\gamma$  = thermal conductance of the ice/snow



# Heat balance equation/ MODIS LIST/ One-Dimensional Thermodynamic Ice Model

$$\cancel{(1 - \alpha)F_r} - I_0 - F_l^{up} + F_l^{dn} + F_s + F_e + F_c = F_a$$

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( $F_a$  assumed to be zero)

$$F_c = \gamma (T_f - T_s)$$

$$\gamma = (k_i k_s) / (k_s H + k_i h)$$

$k_i, k_s \propto$  snow deph and density  
Snow density = 330 kg/m<sup>3</sup>

$T_f$  = freezing temperature

$T_s$  = MODIS night-time LIST observations

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$$H_i = \frac{k_i \times k_s - \left( \frac{F_c}{T_s - T_f} \times k_i \times h_s \right)}{\frac{F_c}{T_s - T_f} \times k_s}$$

$k_i, k_s \propto$  snow depth and density  
Snow density = 330 kg/m<sup>3</sup>

$T_f$  = freezing temperature

$T_s$  = MODIS night-time LIST observations

$\gamma$  = thermal conductance of the ice/snow

$k_i, k_s$  = Ice and snow conductivity

$H$  = Ice thickness

$h$  = snow depth from CLIMo parameterization

# Canadian Lake Ice Model (CLIMo)

## Inputs

Air temperature

Relative humidity

Wind speed

Cloud cover

Snow fall

## Model simulation

### 5 scenarios

1- 100% snow

2- 75% snow

3- 50% snow

4- 25% snow

5- 0% snow

## Outputs

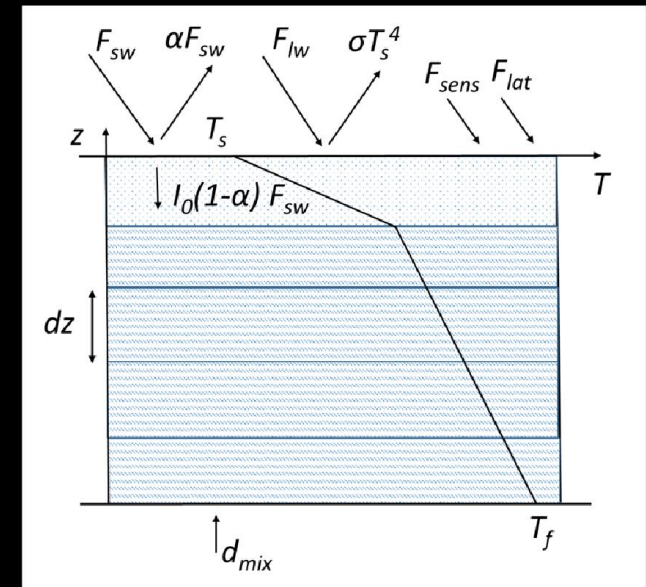
Energy balance components

On-ice snow depth

Annual break up /freeze up

Ice thickness

Temperature profile (snow/ice)





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Air temperature

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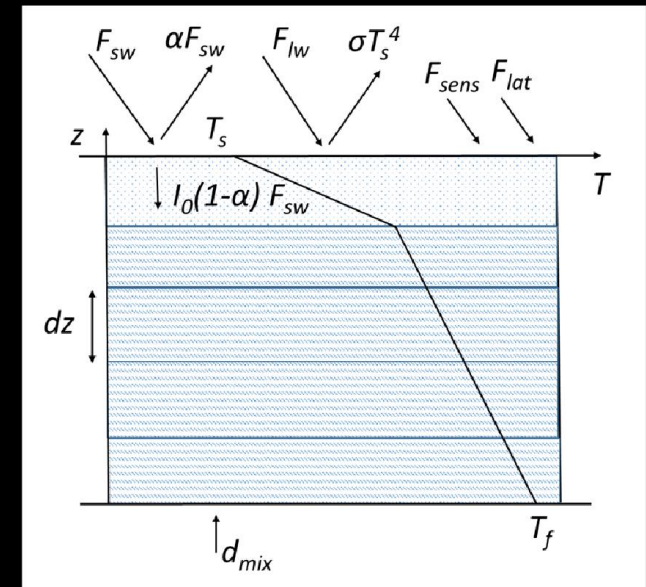
Energy balance components

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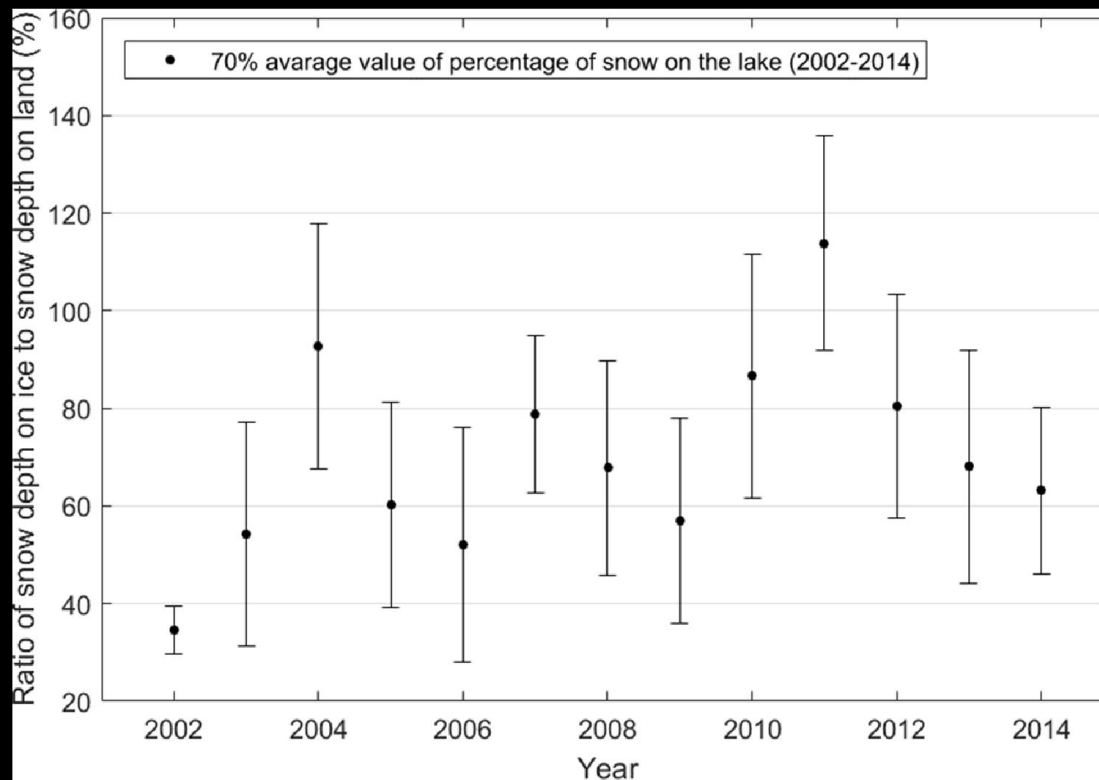
Annual break up /freeze up

Ice thickness

Temperature profile (snow/ice)

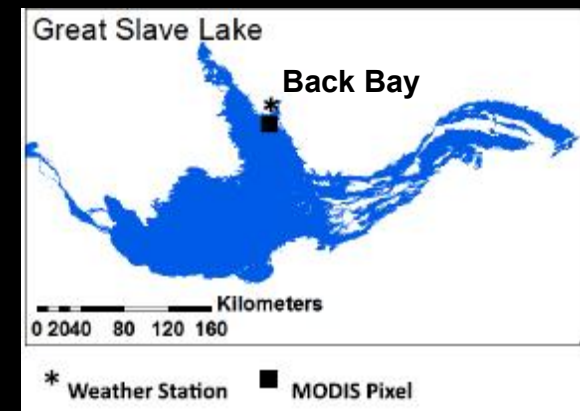


## ***Calculated ice thickness from MODIS vs. in-situ ice thickness (GSL)***



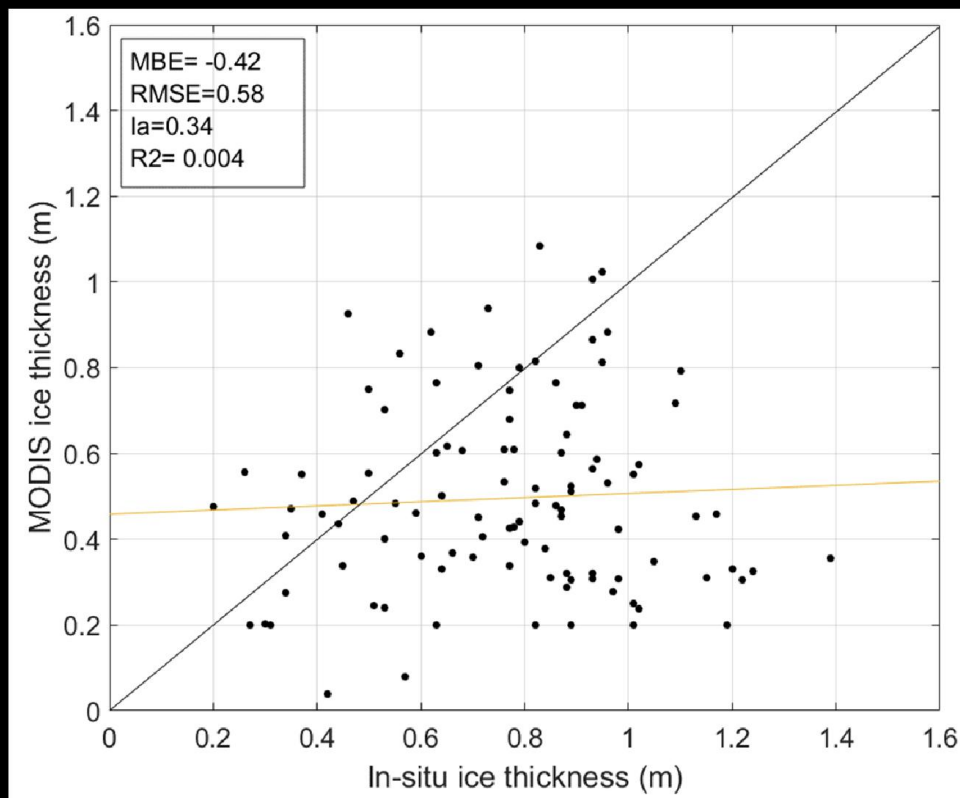
Dots represent average percentage of snow depth on lake for each year and bars are standard deviation.

Percentage of snow depth on lake ice vs. snow depth on the ground at Back Bay weather station (2002–2014).

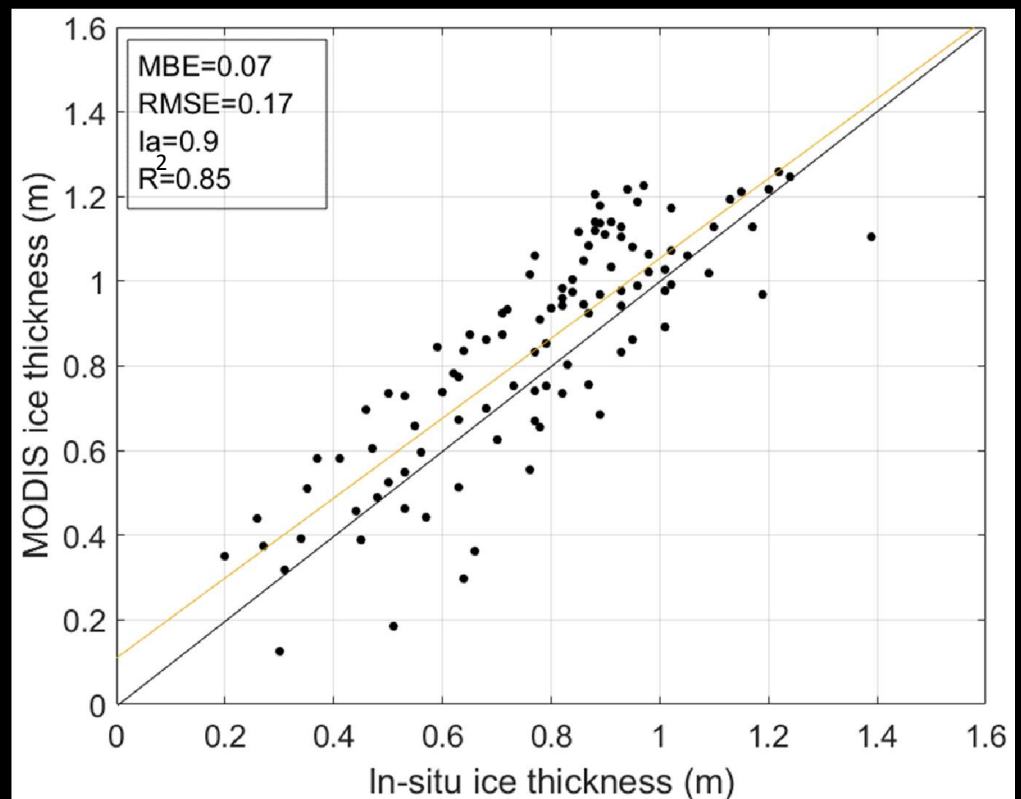


## ***Estimated ice thickness from MODIS vs. in-situ ice thickness (Great Slave Lake)***

Using empirical relationship of snow depths



Using CLIMo parameterization

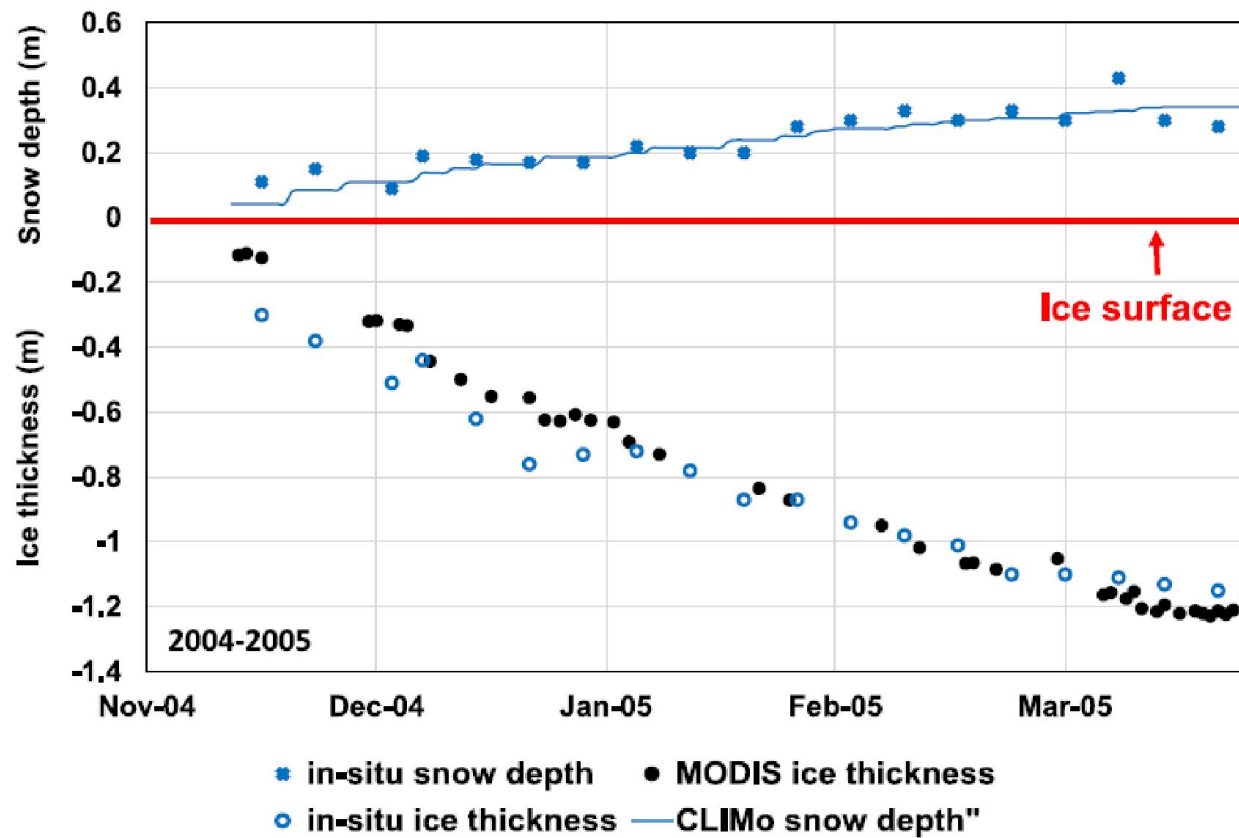


The unit of MBE and RMSE is meter.

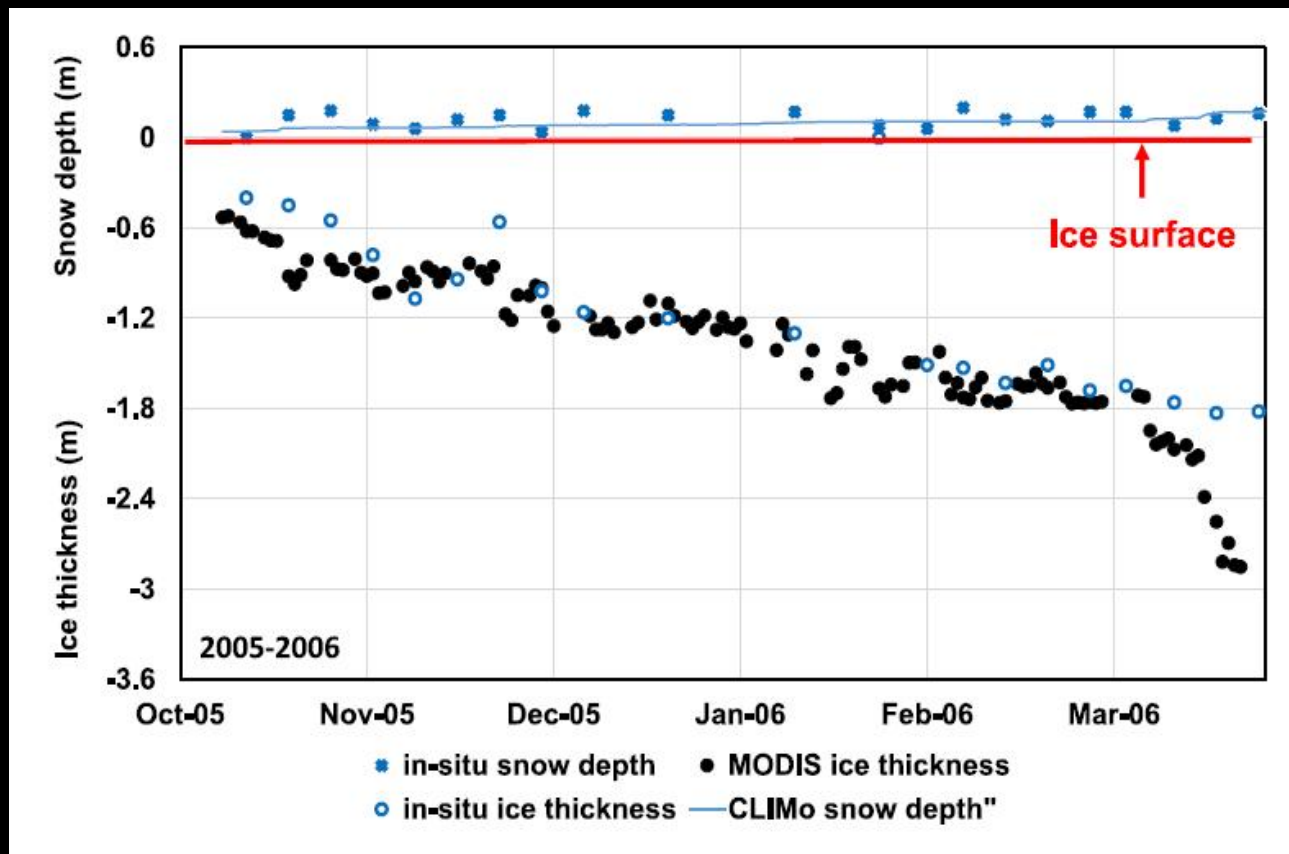
Orange solid line is the correlation fit and the black line is the 1:1 line.



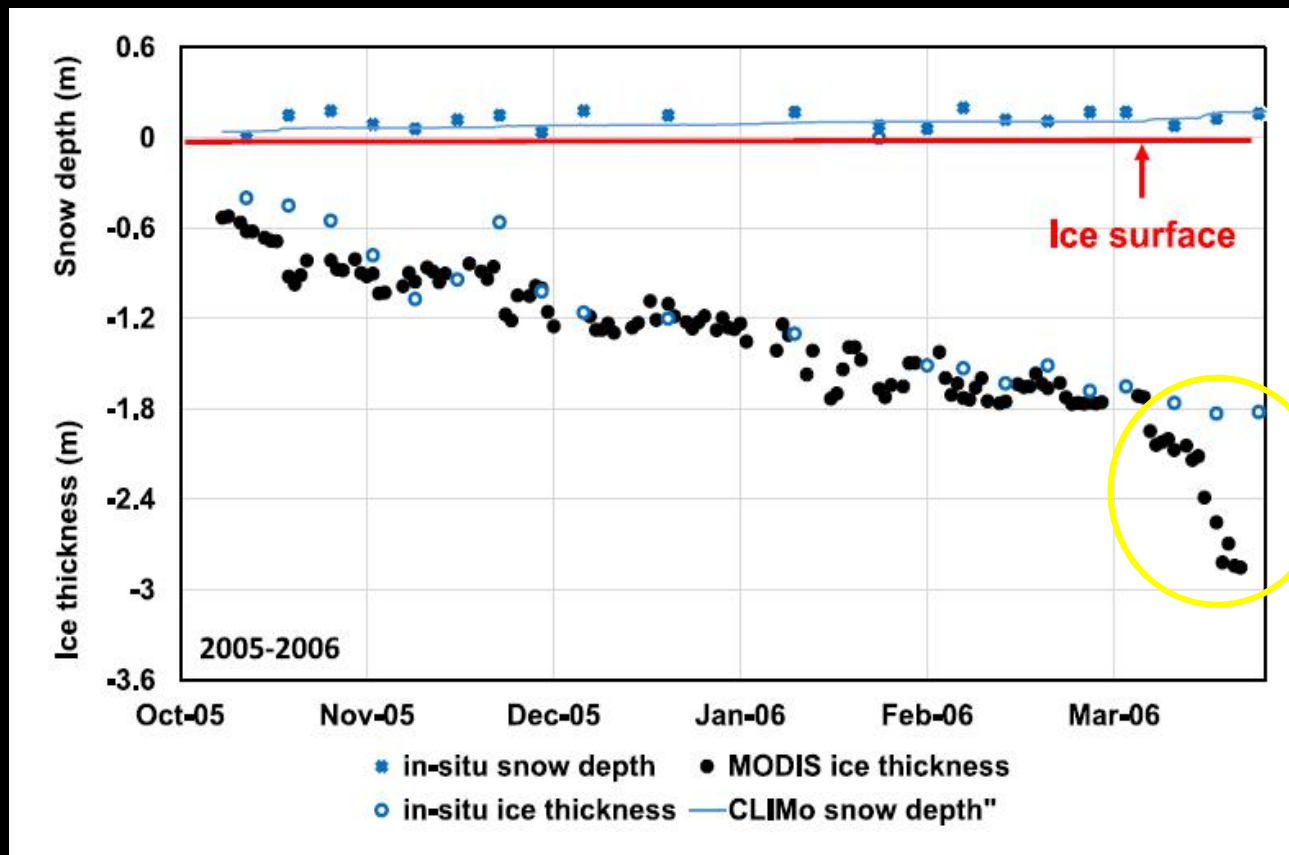
## *Snow and ice thickness from MODIS vs. in-situ ice thickness Great Slave Lake*



## *Snow and ice thickness from MODIS vs. in-situ ice thickness Baker Lake*

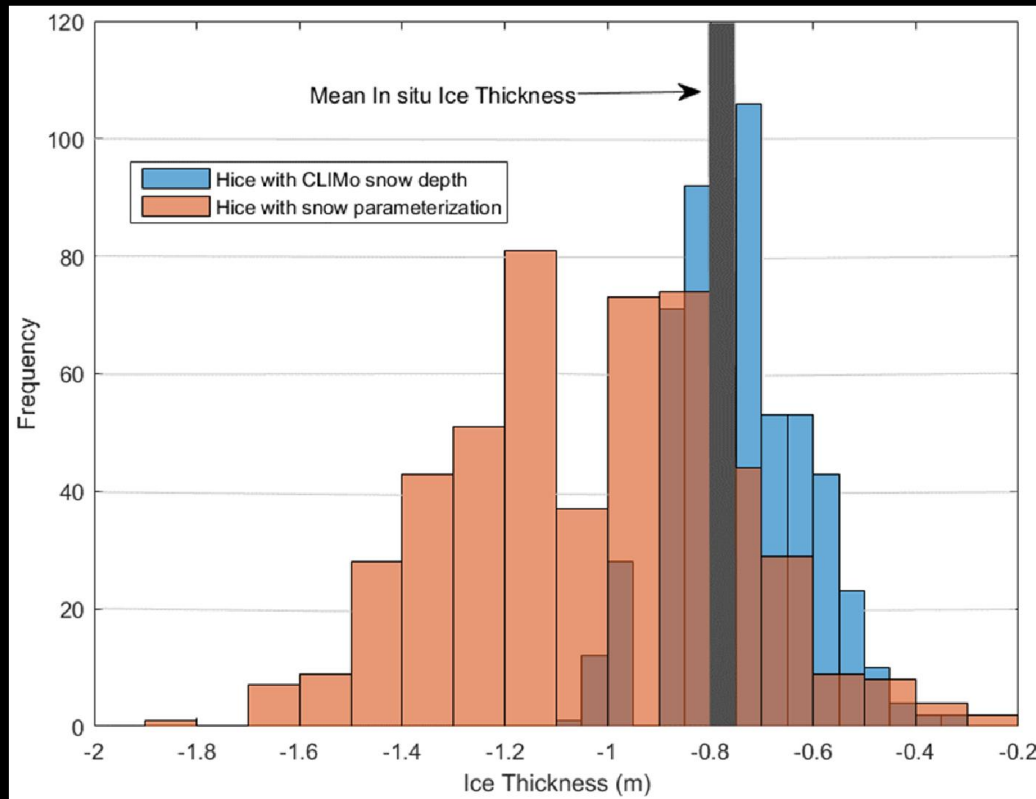


## *Snow and ice thickness from MODIS vs. in-situ ice thickness Baker Lake*



**When accurate snow depth information is available, ice of thickness up to 1.7 m can be retrieved**

## *Sensitivity of the snow depth ice thickness retrieval to the heat flux*



Mean ice thickness value calculated from **empirical snow depth** is farther from the in situ mean ice thickness value vs. mean ice thickness value calculated from **CLIMo** parameterization



## *Sensitivity of the snow depth ice thickness retrieval to the heat flux*

<i>February 2006</i>	$\overline{LIST}(K)$	$\overline{Hs}(m)$	$\delta Hs (m)$	$\overline{Fc} (W/m^2)$	$\delta Fc (W/m^2)$	$\overline{Hi} (m)$	$\delta Hi (m)$	$\delta Hi/\overline{Hi}$
<b>EXP1</b>	251.8	0.21	--	9.94	1.65	0.7	0.07	0.05
<b>EXP2</b>	251.8	0.21	0.07	9.94	--	0.9	0.1	0.12
<b>EXP3</b>	251.8	--	--	9.94	1.65	1.02	0.18	0.17

**EXP1:** *Hs* constant, *Fc* varied by choosing 500 samples from a distribution  $N(\overline{Fc}, \delta Fc)$ .

**EXP2:** *Fc* constant, *snow depth* varied by choosing 500 samples from a distribution  $N(\overline{Hs}, \delta Hs)$ .

**EXP3:** *Fc* varied by choosing 500 samples from a distribution  $N(\overline{Fc}, \delta Fc)$  and the *Hs* used empirical relationship of snow depths and ice thickness.

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## *Sensitivity of the snow depth ice thickness retrieval to the heat flux*

### *Conclusion*

<i>February 2006</i>	$\overline{LIST}(K)$	$\overline{Hs}(m)$	$\delta Hs (m)$	$\overline{Fc} (W/m^2)$	$\delta Fc (W/m^2)$	$\overline{Hi} (m)$	$\delta Hi (m)$	$\delta Hi/\overline{Hi}$
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Comparing the standard deviation of ice thickness ( $\delta Hi$ ) for **EXP1** and **EXP2** demonstrates that the change in ice thickness was more significant when the snow depth was varied, as compared to the conductive heat flux



## ***Sensitivity of the snow depth ice thickness retrieval to the heat flux***

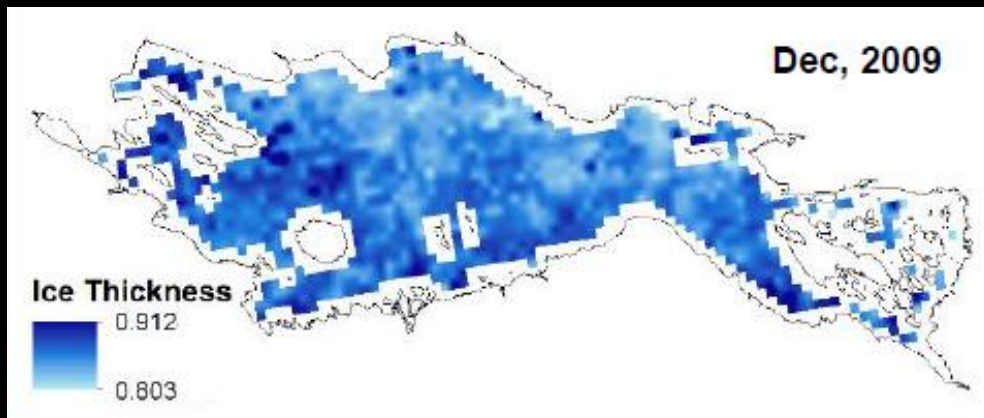
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Comparing  $\delta Hi$  for **EXP1** and **EXP3**, it can be seen that  $\delta Hi$  is larger when the empirical relationship of snow depths is used.

## ***Preliminary result of ice thickness simulation on MODIS LIST pixels***



Cloud cover, wind speed, and surface air temperature were acquired from ERA-Interim which is a global atmospheric reanalysis product provided by ECMWF.



Thanks for your attention!

*Kheyrollah Pour et al. (2017) IEEE Transactions on Geoscience and Remote Sensing, 55, 10, 5956 - 5965.*



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**WATERLOO**



5<sup>th</sup> Workshop on Parameterization of Lakes in Numerical  
Weather Prediction and Climate Modelling

Berlin, Germany, October 16 - 19, 2017



Leibniz-Institute of Freshwater  
Ecology and Inland Fisheries